Few-cycle solitons and supercontinuum generation with cascaded quadratic nonlinearities in unpoled lithium niobate ridge waveguides

Hairun Guo, Xianglong Zeng, Binbin Zhou, and Morten Bache

1DTU-Fotonik, Department of Photonics Engineering Technical University of Denmark, DK-2800, Kgs. Lyngby, Denmark
2Key Laboratory of Special Fiber Optics and Optical Access Networks, Shanghai University, Shanghai 200072, China
3e-mail: zenglong@shu.edu.cn
4e-mail: moba@fotonik.dtu.dk

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Formation and interaction of few-cycle solitons in a lithium niobate ridge waveguide are numerically investigated. The solitons are created through a cascaded phase-mismatched second-harmonic generation process, which induces a dominant self-defocusing Kerr-like nonlinearity on the pump pulse. The inherent material self-focusing Kerr nonlinearity is overcome over a wide wavelength range, and self-defocusing solitons are supported from 1100 to 1900 nm, covering the whole communication band. Single cycle self-compressed solitons and supercontinuum generation spanning 1.3 octaves are observed when pumped with femtosecond nanojoule pulses at 1550 nm. The waveguide is not periodically poled, as quasi-phase-matching would lead to detrimental nonlinear effects impeding few-cycle soliton formation. © 2014 Optical Society of America

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Waveguides in quadratic nonlinear crystals are of great interest because the waveguide will provide strong confinement on the light and suppress the spatial diffraction, which equivalently promotes the efficiency of the nonlinear interaction and therefore pulses with low energy could be operated. With the quadratic nonlinearity giving rise to second-harmonic generation (SHG), or more generally a three-wave mixing (TWM) process, quadratic waveguides find applications in the field of integrated waveguide optics and fiber communications for, e.g., frequency doubling, or frequency upconversions/downconversions. In most cases the waveguides are prepared for noncritical interactions (so-called type-0 interaction, where all waves in the TWM process are identically polarized), which exploits the largest quadratic tensor components but unfortunately cannot be phase-matched. Quasi-phase-matching (QPM) is therefore used to remove the residual phase mismatch and achieve an effective phase-matching condition. Using QPM extends the wavelength range for sum- and difference-frequency generation [1], and extends the phase-matching bandwidth for optical parametric oscillators and amplifiers [2].

On the contrary, in strongly phase-mismatched conditions quadratic nonlinearities produce a so-called cascaded quadratic nonlinearity [3], which acts like a cubic Kerr self-phase modulation (SPM) nonlinearity in inducing an intensity-dependent nonlinear phase shift on the pump pulse. The equivalent Kerr-like nonlinear index is

\[ n_{2,\text{casc}} \propto -d_{\text{eff}}/\Delta k \]

where \( d_{\text{eff}} \) is the effective quadratic nonlinearity and the phase mismatch is \( \Delta k = k_2 - 2k_1 \), where \( k_1 \) and \( k_2 \) are the pump and SH wavenumbers, respectively. This will directly compete with the inherent material self-focusing Kerr nonlinearity \( n_{2,\text{Kerr}} > 0 \), resulting in an effective nonlinear index change \( \Delta n = n_{2,\text{eff}} = (n_{2,\text{casc}} + n_{2,\text{Kerr}}) \). When achieving an effective self-defocusing \( n_{2,\text{eff}} < 0 \) nonlinearity, bulk quadratic materials have received much attention for few-cycle pulse compression, soliton formation, and soliton-induced supercontinuum generation (SCG) of energetic femtosecond pulses [4–7], where the absence of self-focusing effects implies that much more energetic pulses can be used than in traditional Kerr media. Similarly, in quadratic waveguides soliton-induced SCG has been demonstrated in lithium niobate (LN) waveguides [8–9] pumped in the near-IR where LN has normal dispersion. Thus, soliton formation is only possible because the effective nonlinearity is self-defocusing due to a dominant negative cascading nonlinearity. These waveguide studies used type-0 interaction and QPM to reduce the residual phase mismatch and thereby increase \( n_{2,\text{casc}} \). However, it was recently shown [7] that QPM is often detrimental because the cascaded quadratic nonlinearity response can become resonant [10], implying a narrow-bandwidth nonlinearity that impedes nonlinear optics on the few-cycle scale. Moreover, reducing the effective \( \Delta k \) also gives a much stronger cascading-induced pulse self-steepening [11]. In other words, using QPM in tailoring the cascaded quadratic nonlinearity is a two-edged sword; even if it may increase the cascading nonlinearity it will also lead to detrimental nonlinear effects.

In this Letter, we show that, without a QPM structure, a commercial LN ridge waveguide could also have a non-resonant effective self-defocusing nonlinear index, and supports the formation of self-compressed few-cycle solitons in the near-IR. This is achieved through a dominant negative cascaded quadratic nonlinearity (see the diagram in Fig. 1). The waveguide is based on the direct bonding of a LN layer to a lithium tantalate (LT) substrate and then is doped to have a ridge profile [12–13]. Since the LN core and the LT substrate have similar effective refractive index (RI), the waveguide dispersive phase (mode propagation constant) is restricted to be close to the material phase, which makes the phase-mismatch
show effective RIs of extraordinary eigenmodes (with the electric field polarized along the crystallographic z-axis). As guided modes, they should have the effective RI lying between the substrate RI and the core RI. Since the LN core and the LT substrate have small RI difference, the confinement of the waveguide is quite weak and the eigenmodes are restricted to a narrow strip of the effective RIs, which results in two consequences: (1) the mode effective RIs and mode cutoff wavelengths will become sensitive to the waveguide (core) size; (2) the effective RI profiles (especially for the fundamental TM\(_{00}\) mode) as well as the dispersion properties remain close to the material profile as there is little room for variation.

A normalized propagation constant is defined to help remove the material dispersion and to better illustrate the eigenmodes in the waveguide: \( B = (n_{\text{eff}}^2 - n_{\text{sub}}^2)/(n_{\text{core}}^2 - n_{\text{sub}}^2) \) [14], with \( n_{\text{eff}}, n_{\text{core}}, \) and \( n_{\text{sub}} \) representing the mode effective RI, the LN core RI, and the LT substrate RI, respectively. Figure 2(b) shows that with a decreasing core size the fundamental mode is strongly impacted and its cutoff wavelength is shortened as the waveguide confinement is further reduced. Meanwhile, the group velocity dispersion (GVD coefficient \( \beta^{(2)} = d^2\phi/d\omega^2 \)) profiles tend to follow the material profile except for a deflection around the cutoff wavelength, see Fig. 2(c), as there the effective RI is approaching and turning into the substrate RI and a large waveguide dispersion is produced. For structures S-1, S-2 and S-3, the fundamental mode will have both normal and anomalous GVD regions, transiting at a single zero dispersion wavelength (ZDW), which is close to the material ZDW around 1900 nm. Fundamental modes in structures S-4 and S-5 have very short cutoff wavelengths so that they just have normal GVD regions.

We now estimate the nonlinearities in the waveguide. The relevant cascaded nonlinearity is represented as the nonlinear coefficient \( \gamma_{\text{casc}} = (\omega/c)(n_{\text{casc}}/A_{\text{eff,casc}}) \) [15], which is analogous to the material Kerr nonlinearity scaled as \( \gamma_{\text{Kerr}} = (\omega/c)(n_{\text{Kerr}}/A_{\text{eff,Kerr}}) \) [16], where \( A_{\text{eff,casc}} \) and \( A_{\text{eff,Kerr}} \) are effective mode areas corresponding to the cascaded nonlinearity and the Kerr nonlinearity, respectively. It should be noted that \( A_{\text{eff,casc}} \) actually stems from a SHG process and therefore has a different definition to the commonly known \( A_{\text{eff,Kerr}} \) from a Kerr SPM process. A dispersive \( A_{\text{eff,casc}} \) referring to the SHG within the TM\(_{00}\) mode is defined as [15]

\[
A_{\text{eff,casc}}(\omega_1) = \frac{1}{2} \left( \frac{\int d\omega_1 |U_{\text{TM}_{00}}(\omega_2)|^2}{\int d\omega_1 |U_{\text{TM}_{00}}(\omega_1)|^2} \right)^2 \left( \frac{\int d\omega_2 |U_{\text{TM}_{00}}(\omega_2)|^2}{\int d\omega_2 |U_{\text{TM}_{00}}(\omega_1)|^2} \right)^2,
\]

where \( U_{\text{TM}_{00}} \) is the eigenmode distribution of the TM\(_{00}\) mode, \( \omega_1 \) and \( \omega_2 \) are angular frequencies of the pump and the SH. \( A_{\text{eff,casc}} \) as a function of the pump wavelength is illustrated in Fig. 3(a), which is quite close to the \( A_{\text{eff,Kerr}} \) referring to the Kerr SPM process within the TM\(_{00}\) mode. Other effective mode areas stemming from interactions among high-order modes (also phase-mismatched) are much larger than the two shown due
of the waveguide is then calculated as $L_N = |P \cdot r_{\text{eff}}|^{-1}$, where $P$ is the peak power of the pump pulse. Furthermore, with the dispersion length $L_D = T_0^2/|\beta_2|^2$ ($T_0$ is the pulse duration), the soliton number $N$ can be finally estimated as $N^2 = L_D/L_N$.

Now we numerically investigate the few-cycle soliton formation in an LN ridge waveguide. The numerical model is the nonlinear wave equation in frequency domain (NWEF), which accurately models ultrashort pulse propagation in nonlinear materials [19]. In waveguides, the NWEF is actually governing the propagation dynamics of the pulse electric field amplitude while the pulse transverse distribution is described in form of waveguide eigenmode distributions [20].

We first show pumping at 1550 nm where the total self-defocusing nonlinearity is maximum. The input pulse has 10-nJ energy, 50-fs FWHM, and it is in the TM$_{00}$ mode. During the propagation, the pulse spectrum evolves with SPM-induced spectral broadening. Meanwhile, a soliton-induced optical Cherenkov wave (or dispersive wave, DW) [21] is generated at opposite GVD region around 3000 nm due to the perturbation of higher-order dispersion, see Figs. 4(a) and 4(b). Combined with the normal dispersion, the ultrabroad spectrum leads to the formation of a single-cycle self-compressed soliton. In Fig. 4(c), the pulse profile with significant compression while its peak power is enhanced over 6 times. After the compression, the pulse is split into several branches due to the Raman fraction (~50%) in the LN material, known as the Raman-induced pulse splitting [22]. Figure 4(d) shows the electric field amplitude of the compressed pulse, with clean and single-cycle profile. The quality factor (defined in [17]) is around 0.4. Actually, to the orthogonality among different modes, and the corresponding nonlinear factors $\gamma$ are therefore largely reduced and negligible.

Figure 3(b) shows that the negative nonlinear cascading factor $\gamma_{\text{casc}}$ for the TM$_{00}$ mode is stronger than the Kerr nonlinear factor $\gamma_{\text{Kerr}}$ over a broad wavelength span (1100–3000 nm). Such a broadband self-defocusing nonlinearity is actually built up due to the large susceptibility $d_{33}$ of the LN material, which gives rise to a dominant $n_{2,\text{casc}}$ [7]. However, such a self-defocusing nonlinearity should work with the normal GVD to excite solitons, so the window of operation is actually from 1100 nm to the GVD transition position at 1900 nm. Within such a “compression window” [17] the phase-mismatch parameter is actually below the critical value $\Delta k_c$, referring the balance between the cascaded and the Kerr nonlinearity, see Fig. 3(c). Meanwhile, the phase mismatch is larger than the threshold $\Delta k_{\text{th}}$ to the resonant regime, which means the cascaded response is ultrafast, broadband, and without the characteristic resonant spectral peaks generated if $\Delta k$ is in the marked area [10,18,19]. Therefore, we may expect few-cycle soliton formation with high pulse quality. Unlike most LN waveguides having QPM to tune the phase mismatch, the presented LN ridge waveguide is actually QPM-free as it is naturally suitable for few-cycle soliton formation, just like the bulk LN case investigated in [7].

Summarizing, the total nonlinearity governing the pulse SPM is $r_{\text{eff}} = r_{\text{casc}} + r_{\text{Kerr}}$. The nonlinear length $\Delta k$ of waveguide is then calculated as $L_N = |P \cdot r_{\text{eff}}|^{-1}$, where $P$ is the peak power of the pump pulse. Furthermore, with the dispersion length $L_D = T_0^2/|\beta_2|^2$ ($T_0$ is the pulse duration), the soliton number $N$ can be finally estimated as $N^2 = L_D/L_N$.

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at other wavelengths and in the other structures, S2 to S5, such scenario of the cascaded quadratic soliton compression also works only if the pump pulse is within the compression window as illustrated above.

Aside from the soliton compression, such a waveguide can also be applied for SCG. By launching a longer pulse with more energy, namely 150-fs FWHM and 30-nJ energy, the soliton number is increased correspondingly to 11.10 and a supercontinuum spectrum covering 1300–3200 nm with 1.3 octave bandwidth (at −10 dB) is accomplished, as shown in Fig. 5. As opposed to SCG in photonic crystal fibers [28], here the combination of self-defocusing nonlinearities and soliton formation in the normal dispersion regime leads to the blue edge of the spectrum being supported by cascading-induced pulse self-steepening [11], while the red-edge formation occurs due to the Raman-induced pulse splitting of the solitons in the nonlinear regime, and soliton-induced DW generation in the linear long-wavelength regime of anomalous dispersion [21].

In summary, we investigated a commercial LN ridge waveguide structure and found that strong cascaded quadratic nonlinearity could be produced through the QPM-free type-0 SHG process in the waveguide. Therefore, the waveguide can be applied for cascaded quadratic soliton compression, which makes use of the self-defocusing nonlinearity combined with normal dispersion. By carefully studying the dispersion properties and the nonlinearities in such a QPM-free waveguide, the compression window is concluded to be from 1100 to 1900 nm, which exactly covers the whole communication band. At 1550 nm, single cycle pulse compression was observed by pumping a low-energy pulse, while when a longer pulse is launched, the waveguide can produce octave-spanning SCG. With compact size, simple structure and high nonlinearities, such a QPM-free quadratic waveguide could have great potential in optical communications and laser physics.

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